

# Mathematical model of the factor H mediated self and non-self discrimination by the complement system

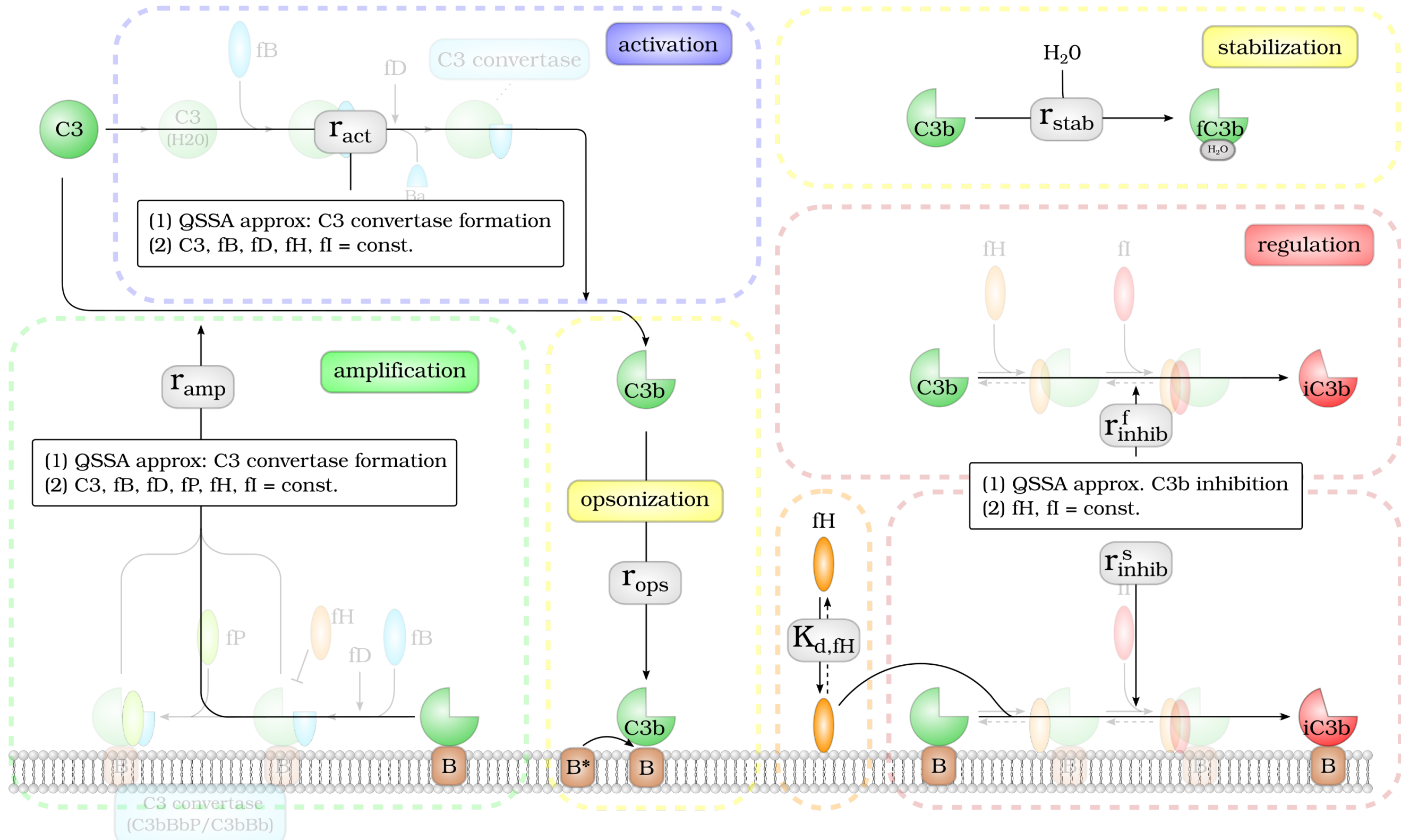
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## complement system

The complement system is a key factor in host defence and its main task is to recognize and opsonize invading microorganisms as well as attracting phagocytes to the site of infection. It comprises a set of plasma proteins that get activated via biochemical reactions on distinct pathways. To protect host cells from opsonization a tight regulation mechanism is needed.



## key molecules

- opsonin C3b:** - forms a molecular complex, that activates new C3b molecules
- regulator factor H (fH):** - plasma protein that can be bound to surfaces
  - accelerates decay of C3b amplification complex
  - mediates C3b degradation

## aims of the mathematical model

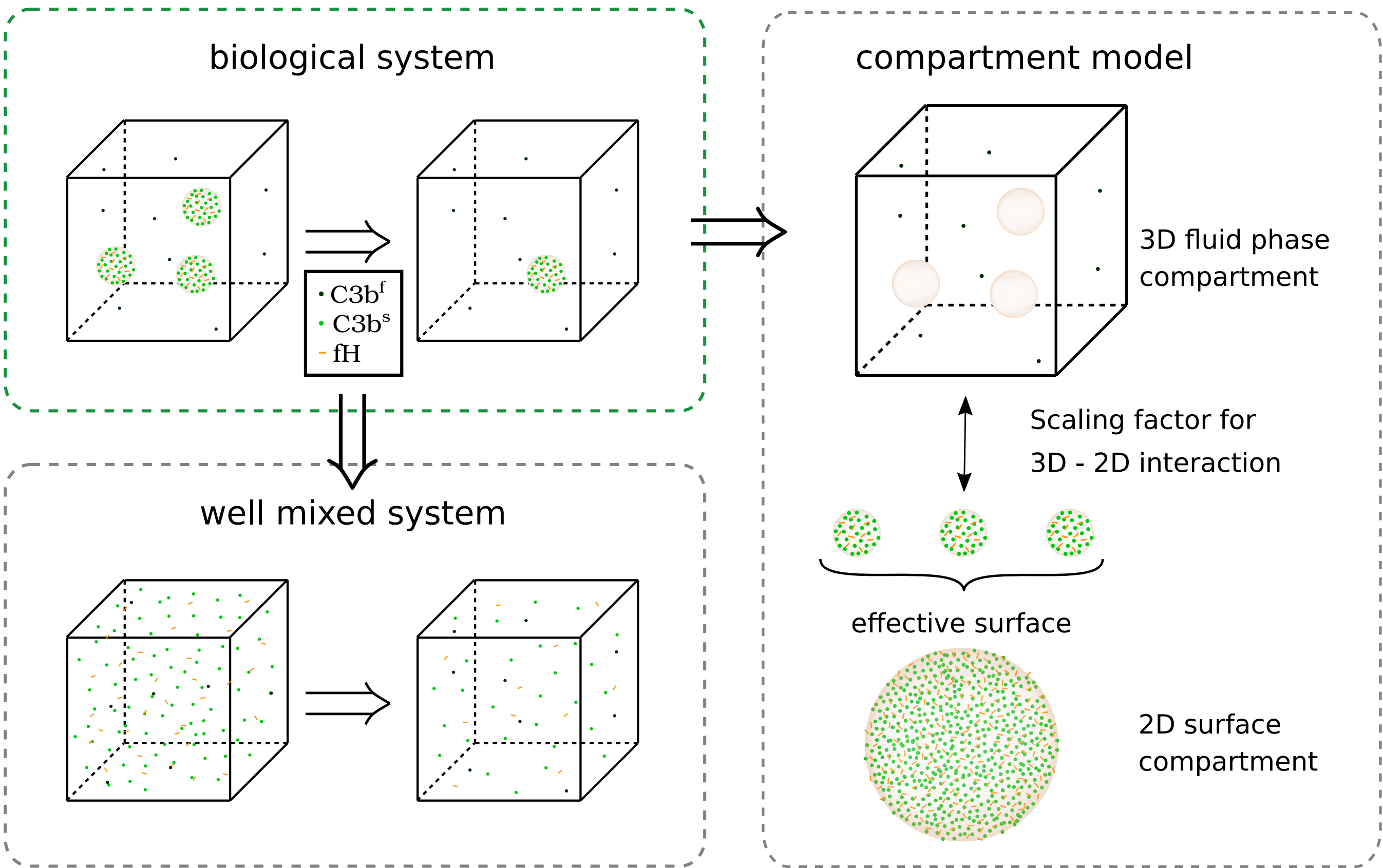
- determine reaction rate by fitting model to experimental data
- determine driving processes of the opsonization mechanism
- predict opsonization level based on concentration of surface bound factor H

## model I: well mixed system

$$\begin{aligned} \frac{d}{dt} C3b^f &= r_{act} + r_{amp}(fH^s, C3b^s) \cdot C3b^s \\ &\quad - r_{ops} \cdot B^*(fH^s, C3b^s) \cdot C3b^f - r_{stab} \cdot C3b^f - r_{inhib}^f \cdot C3b^f \\ \frac{d}{dt} C3b^s &= r_{ops} \cdot B^*(fH^s, C3b^s) \cdot C3b^f - r_{inhib}^s(fH^s, C3b^s) \cdot C3b^s \\ \frac{d}{dt} iC3b^s &= r_{inhib}^s(fH^s, C3b^s) \cdot C3b^s - \mu_{iC3b^s} \cdot iC3b^s \end{aligned}$$

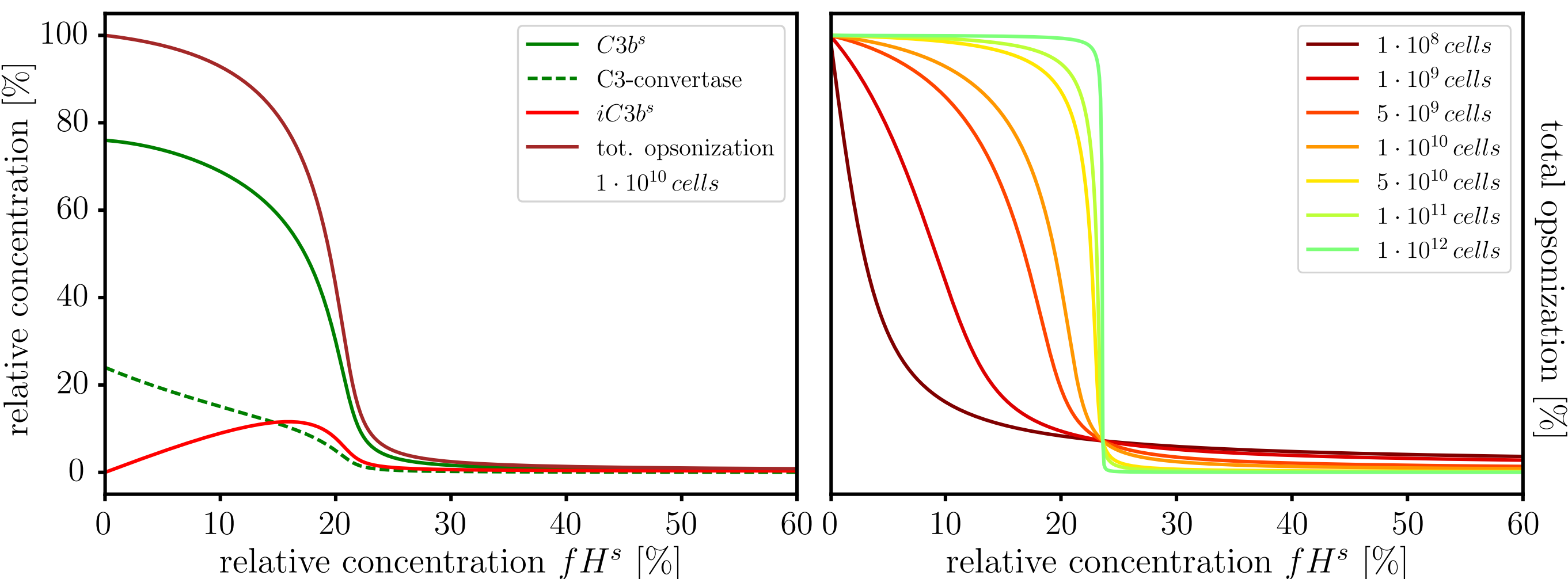
## adding spatial information to the model

- false interpretation of the concentration of surface molecules in well mixed model
- need to include spatial information into the model



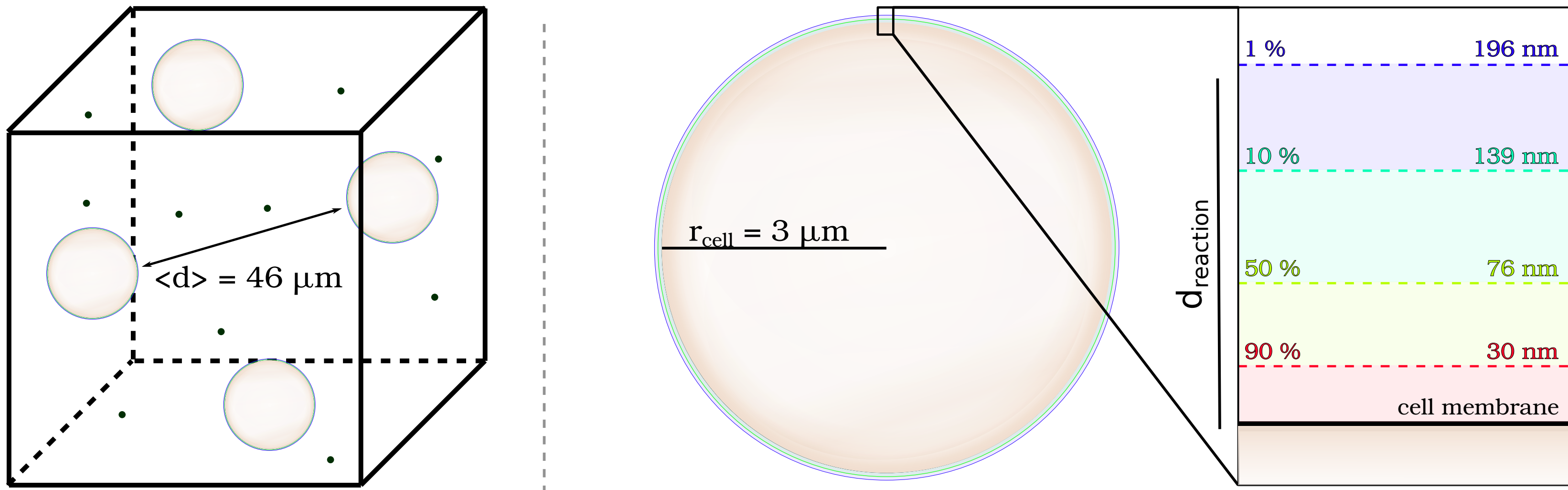
## model II: compartment model of cell interaction

- well representation of surface bound molecules
- concentraon of surface bound molecules in relative units in order to compensate scaling of cell size and numbers
- bimolecular reaction rates on surfaces are not comparable to experimental results due to mismatching units



## model III: modeling a single cell

- short lifetime of active C3b molecules in liquid ( $t_{1/2} = 60\mu s$ )
- mean interparticle distance much larger than the distance a C3b molecule can travel
- amplification on a cell is a local phenomenon and each cell will be modelled individually
- compartment model:
  - 3D compartment including the interaction volume defined by  $d_{reaction}$
  - 2D surface compartment



drawback: - mode depends on artificially introduced parameter  $d_{reaction}$   
- spatial distribution of C3b molecules not well represented

solution: - combination of ODE and PDE to describe spatial distribution in liquid  
- much more complex steady state solution → solve radial Poisson equation

## summary and outlook

	determine reaction rates	determine driving processes	predictions
model I: well mixed system	✗	✗	✗
model II: two compartment model	✓	✓	✓
model III: single cell	✓	✓	✓

Model II and model III can be used to correctly describe the concentration of surface-bound molecules. Experiments will be used to determine which model better describes the biological system. In particular, the question whether the interaction of cells plays a role must be clarified.

